



Abdallah Aoude¹, Ioannis Stefanou¹, Jean-Francois Semblat², Vito Rubino¹

¹Nantes Université, Ecole Centrale Nantes, CNRS, Institut de Recherche en Génie Civil et Mécanique (GeM), UMR 6183, F-44000 Nantes, France

²ENSTA-Paris, Institute of Mechanical Sciences and Industrial Applications

abdallah.aoude@ec-nantes.fr, ioannis.stefanou@ec-nantes.fr, jean-francois.semblat@ensta-paris.fr, vito.rubino@ec-nantes.fr



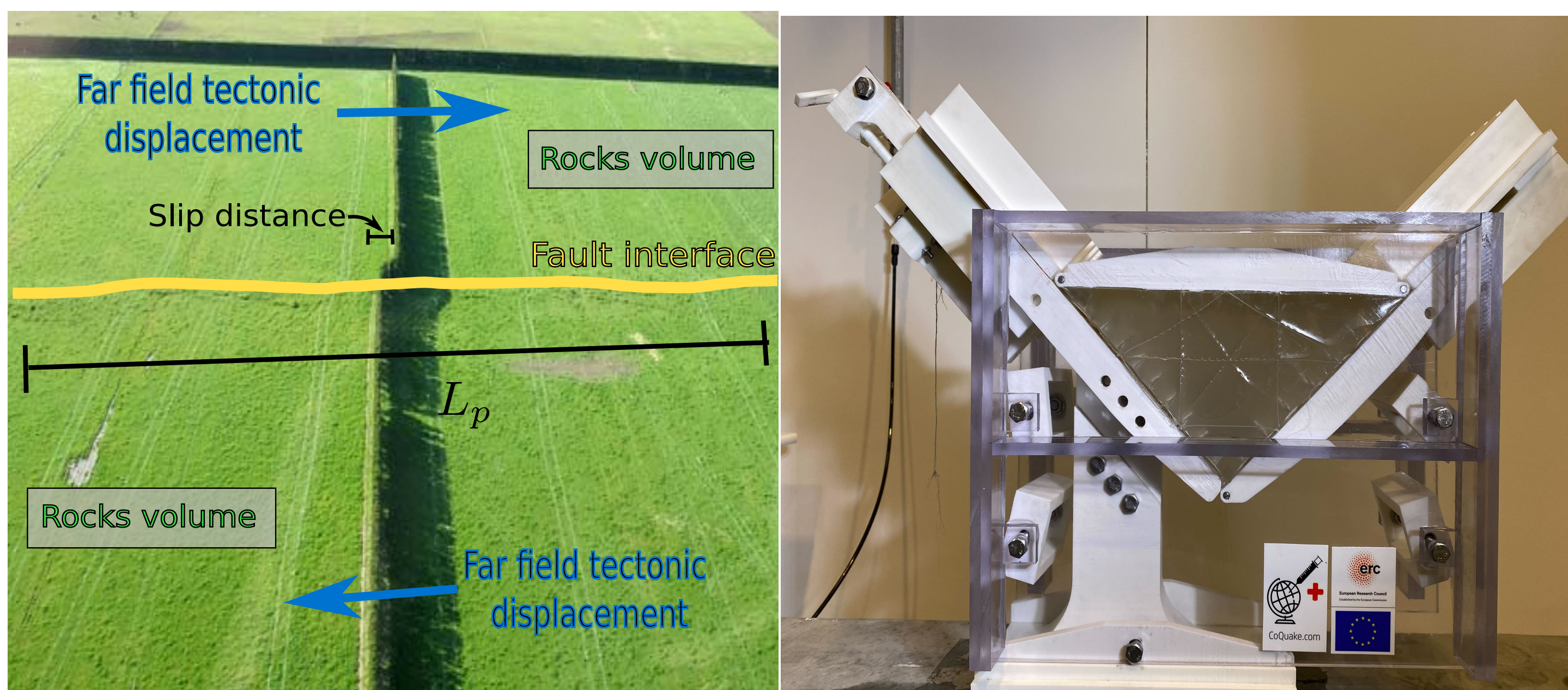
1-Context

Human activities can induce seismicity by injecting fluids into the Earth's crust, as observed in geothermal operations. Recently, it has been demonstrated that controlling the pressure of the injected fluids can mitigate earthquakes. These mitigation strategies are designed using the mathematical theory of control [1-4].

In this study, we present a new experimental setup designed to test the mathematical theory of control. It consists of an analog fault surrounded by an elastic material, enabling us to study slip propagation.

2-Laboratory experiment: Scaling laws

The design is based on scaling rules used to downscale instabilities of earthquakes from natural faults (prototypes) to laboratory (models).



<https://www.geonet.org.nz/news/3G1z0kLuWbwLdrDF6kq5x>

Scaling rules:

$$\lambda_{\Delta\tau} = \frac{\lambda_G \lambda_\delta}{\lambda_L}$$

$$\lambda_t = \frac{\lambda_L}{\lambda_{c_s}}$$

$$\lambda_L = \frac{\lambda_{\Delta\tau}}{\lambda_{M_0}}$$

$$\lambda_X = \frac{\text{model quantity } X_m}{\text{prototype quantity } X_p}$$

Physical quantities	Non-dimensional ratio
$\Delta\tau$ shear stress drop	$\lambda_{\Delta\tau} = \frac{(\Delta\tau)_m}{(\Delta\tau)_p}$
δ slip distance	$\lambda_\delta = \frac{\delta_m}{\delta_p}$
L length scale	$\lambda_L = \frac{L_m}{L_p}$
c_s shear wave velocity	$\lambda_{c_s} = \frac{(c_s)_m}{(c_s)_p}$
G shear modulus	$\lambda_G = \frac{G_m}{G_p}$
M_0 seismic moment	$\lambda_{M_0} = \frac{(M_0)_m}{(M_0)_p}$
t time	$\lambda_t = \frac{t_m}{t_p}$

3-Technical constraints and scenarios

Reference parameters: $G_p = 30$ GPa (Typical shear modulus for rocks), $(\Delta\tau)_p = 3$ MPa (Typical shear stress drop for an earthquake), $L_m^{max} = 0.2$ m (Desired fault length in the laboratory)

Constraints: Minimum time required to sample data and control instabilities, $t_{sample} > 10$ ms; Minimum slip to be measured with sensors $\delta_m^{min} = 0.7$ mm

Scenario 1: Maximum earthquake magnitude $M_w = 4$; Scenario 2: Minimum Earthquake magnitude $M_w = 2$

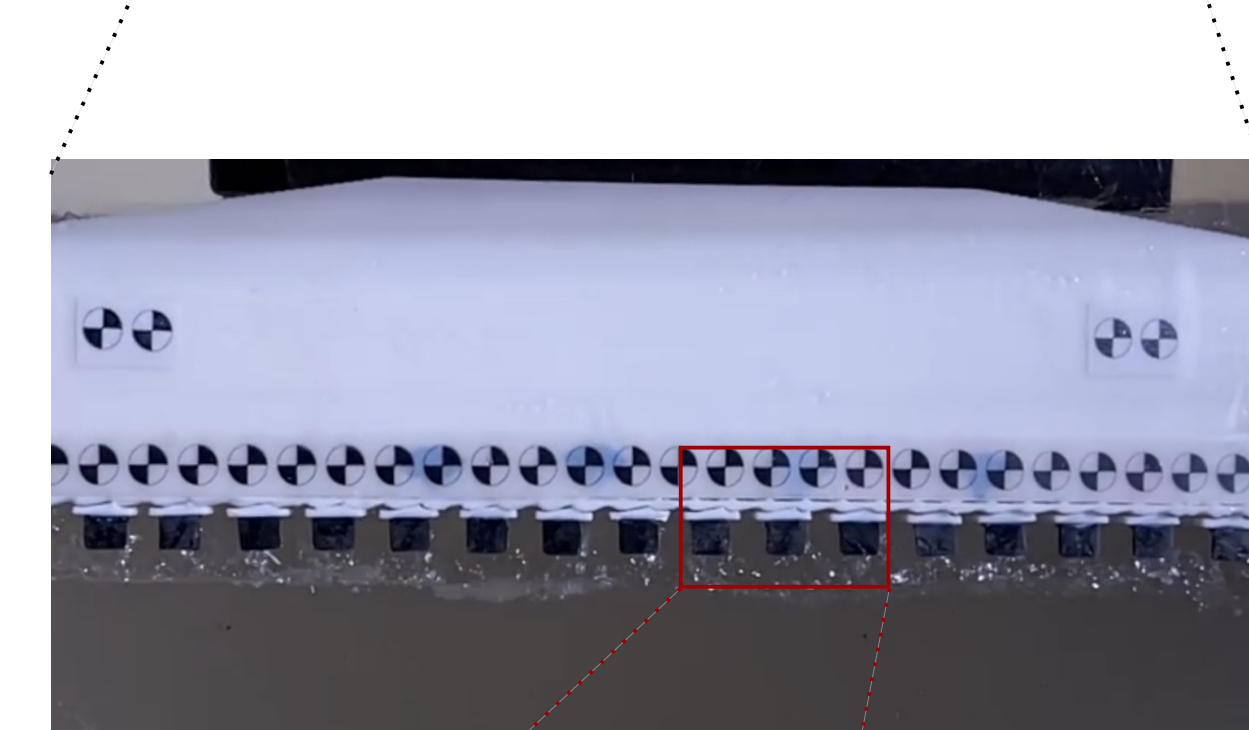
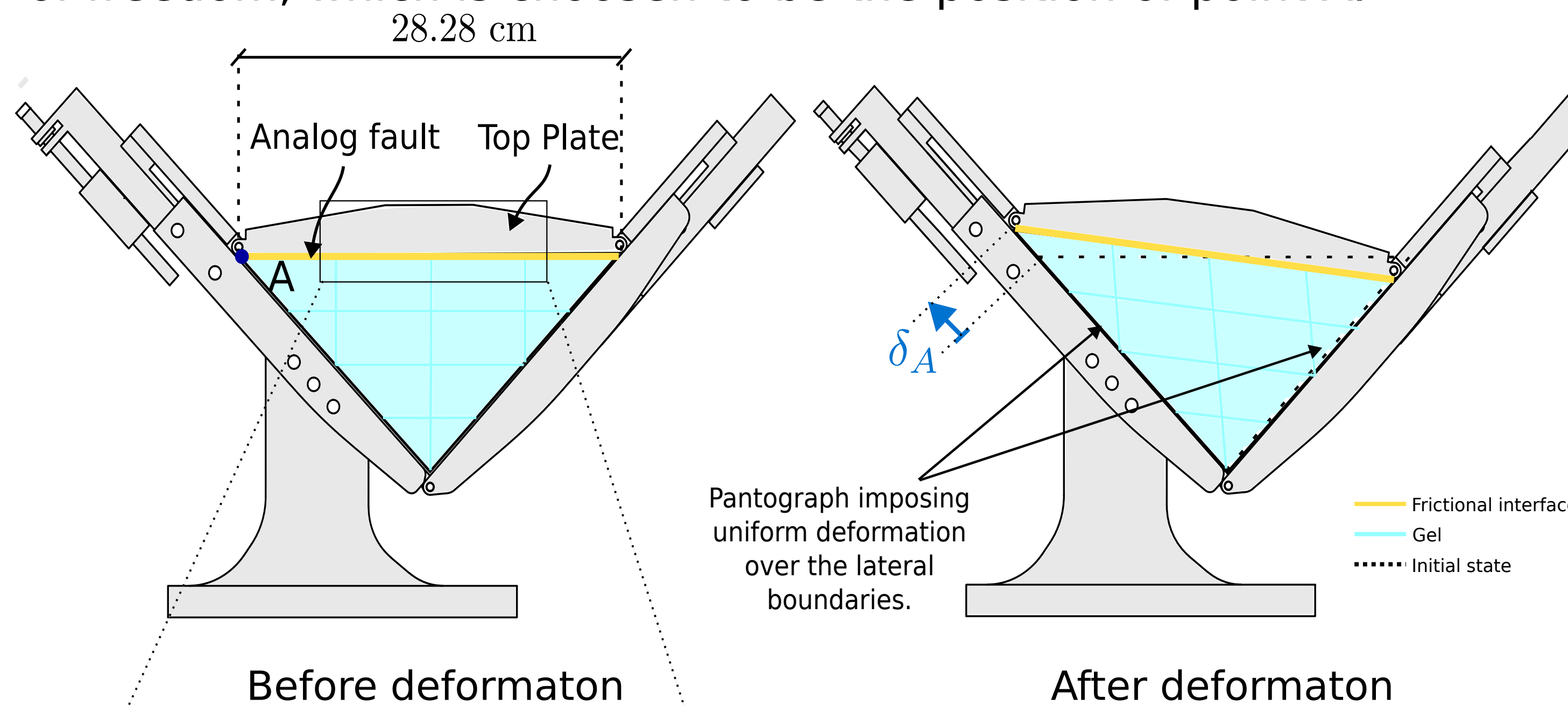
Using empirical equations, L_p for $M_w=4$ is: $L_p^{max} = 1100$ m; for $M_w=2$ is: $L_p^{min} = 110$ m

$\lambda_L = \frac{L_m^{max}}{L_p^{max}} = 1.2 \cdot 10^{-4}$ \rightarrow $L_m^{min} = \lambda_L L_p = 0.02$ m

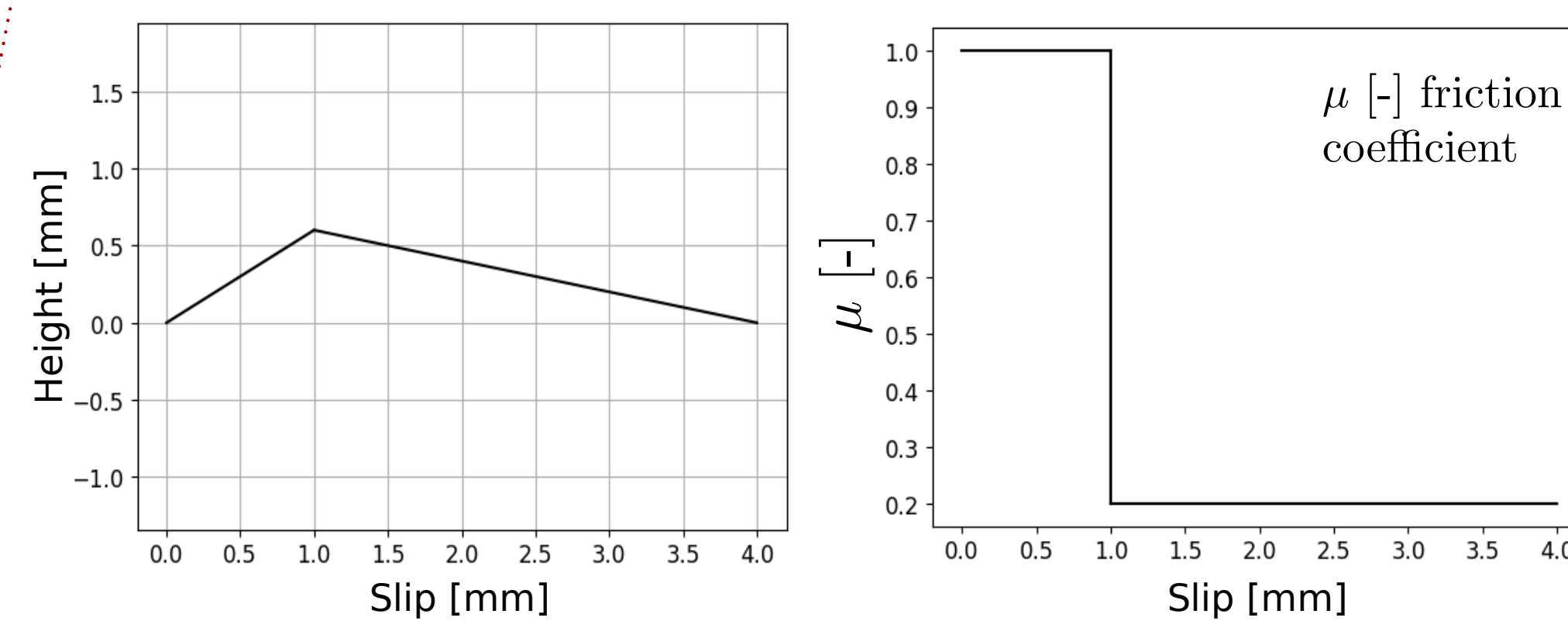
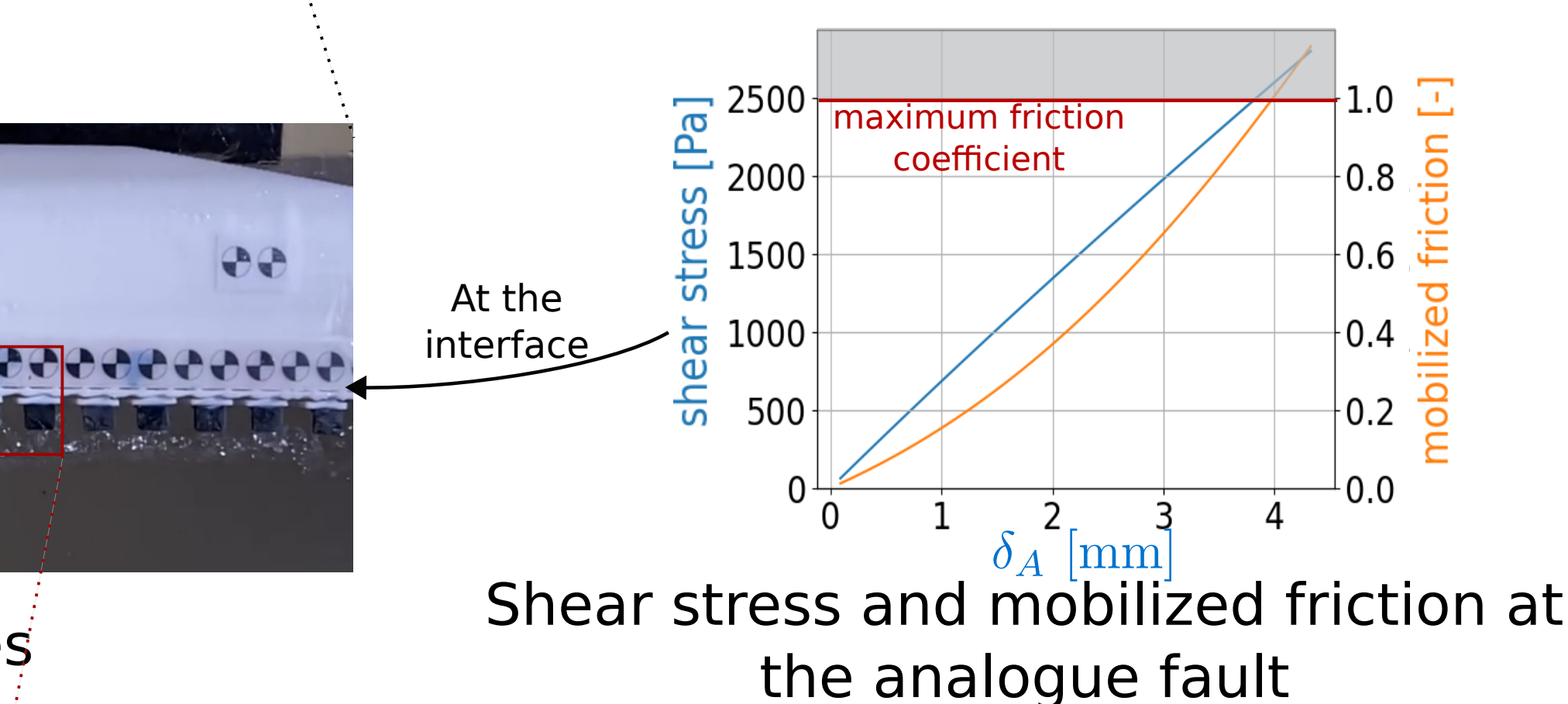
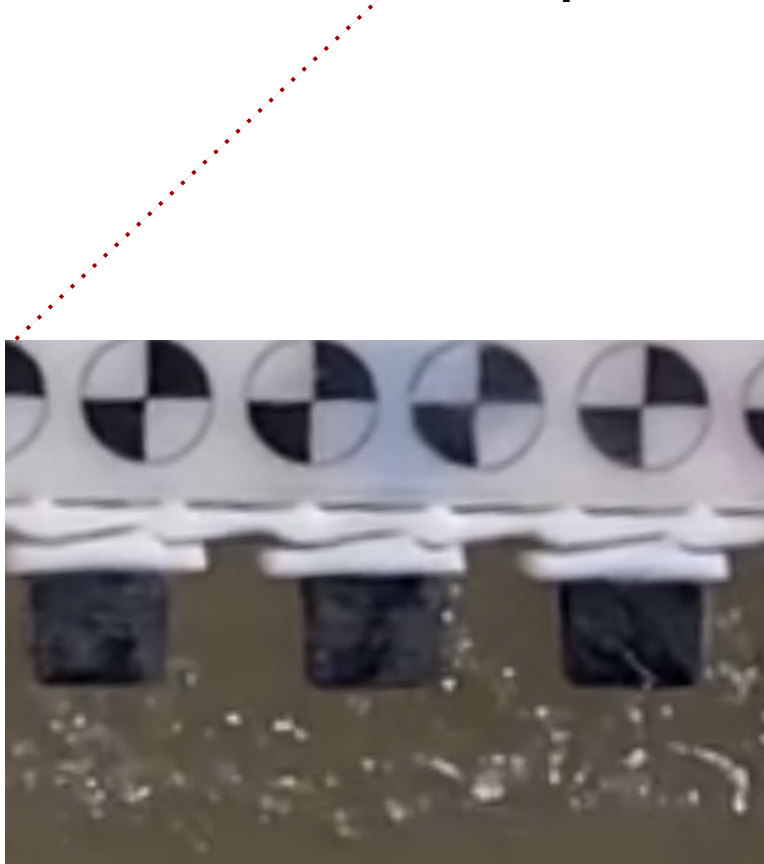
Maximum slip time estimation: $t_m^{max} = 100$ ms; Minimum slip time estimation: $t_m^{min} = 10$ ms

4-Earthquake mechanical apparatus

Assuming the gel is incompressible, the system has a single degree of freedom, which is chosen to be the position of point A.

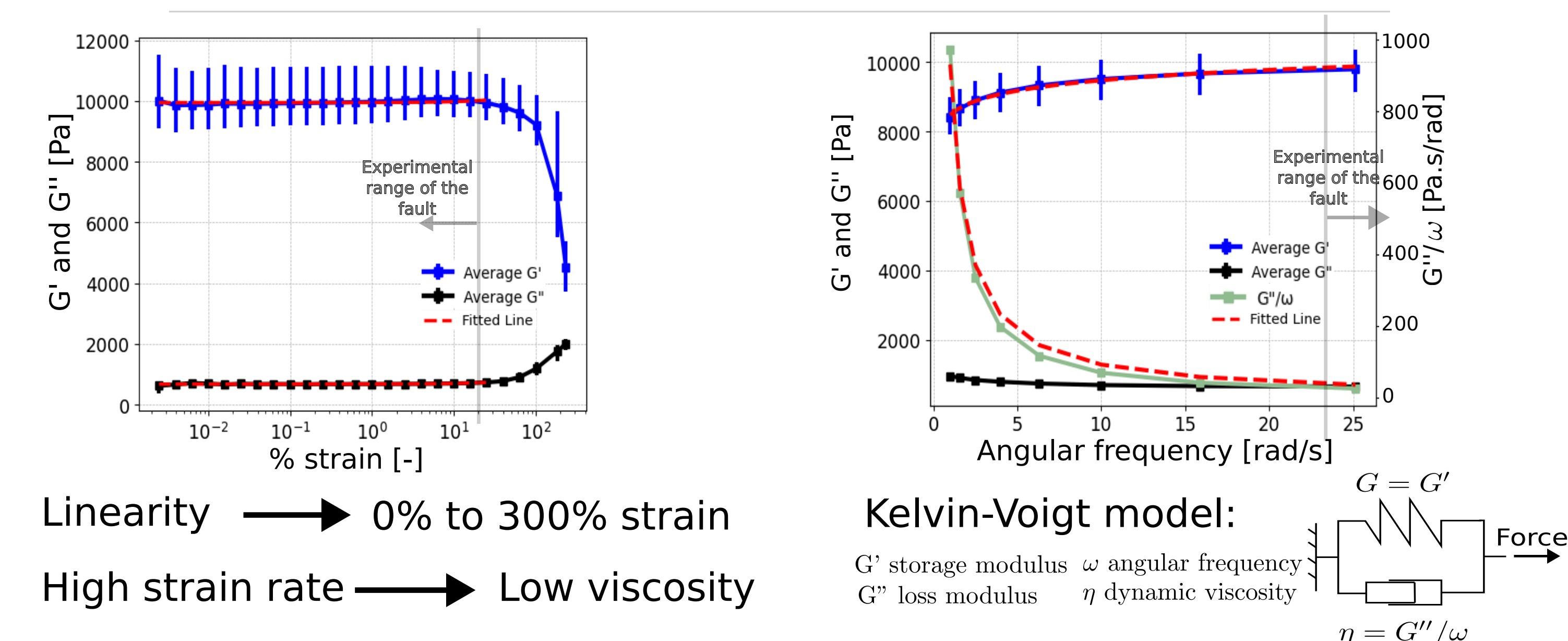


16 patches



Geometric profile of 1 patch and its corresponding frictional evolution with slip

5-Rheology of the gel

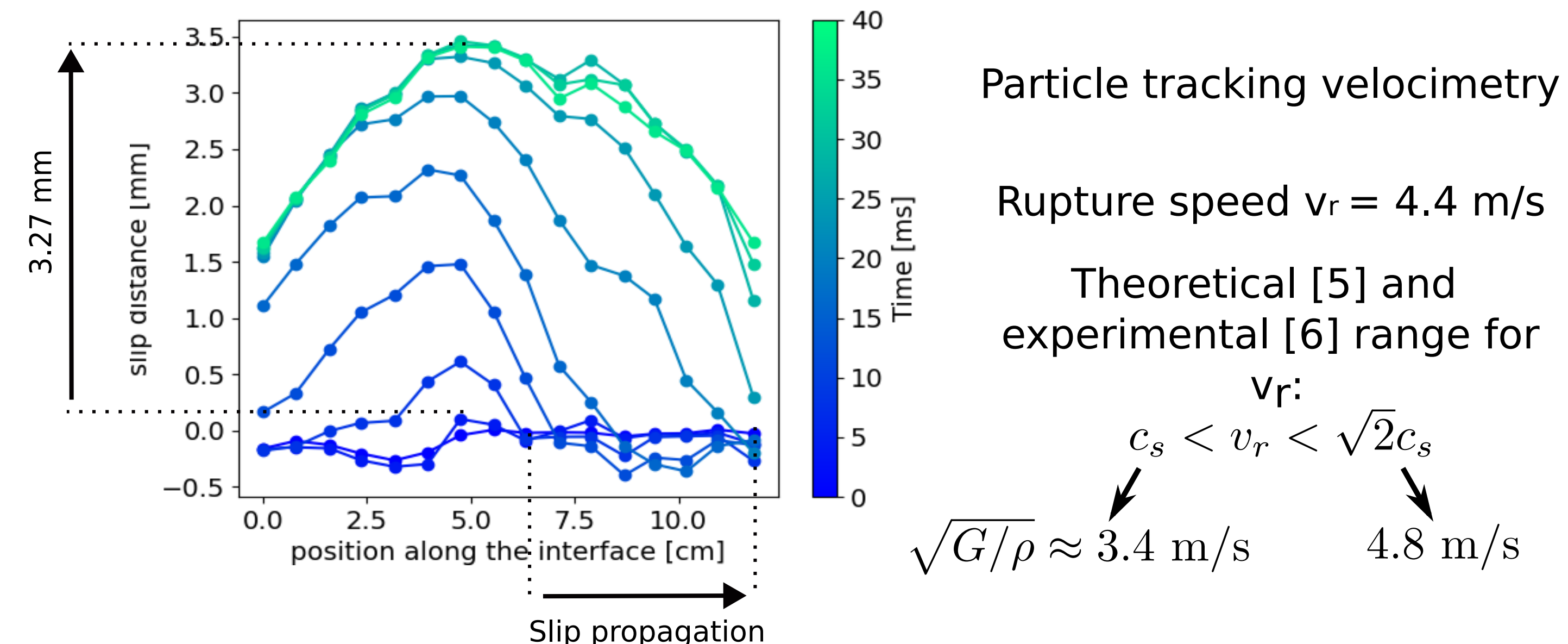


Linearity \rightarrow 0% to 300% strain

High strain rate \rightarrow Low viscosity

Kelvin-Voigt model: $G' = G'$ (storage modulus), $G'' = \eta \omega$ (loss modulus), $\eta = G''/\omega$ (dynamic viscosity)

6-Slip propagation measured experimentally



Particle tracking velocimetry

Rupture speed $v_r = 4.4$ m/s

Theoretical [5] and experimental [6] range for v_r :

$$c_s < v_r < \sqrt{2}c_s$$

$$\sqrt{G/\rho} \approx 3.4 \text{ m/s} \quad 4.8 \text{ m/s}$$

7-Conclusions and perspectives

A new laboratory earthquake experiment is designed, composed of an analogue fault surrounded by elastic media.

Deforming the analog rock increases the shear stress at the interface, thus allowing instabilities to take place.

The slip measured using particle tracking velocimetry propagates at a speed between c_s^{gel} and $\sqrt{2}c_s^{gel}$, as expected.

Next step: adjust the effective stress over the analogue fault using control theory [1-4], to avoid instabilities and achieve controlled slip rates.

References

[1] Stefanou, Ioannis. "Controlling anthropogenic and natural seismicity: Insights from active stabilization of the spring-slider model." Journal of Geophysical Research: Solid Earth 124.8 (2019): 8786-8802. doi: <https://doi.org/10.1029/2019JB017847>

[2] Stefanou, Ioannis, and Georgios Tzortzopoulos. "Preventing Instabilities and Inducing Controlled, Slow-Slip in Frictionally Unstable Systems." Journal of Geophysical Research: Solid Earth 127.7 (2022): e2021JB023410. doi: <https://doi.org/10.1029/2021JB023410>

[3] Tzortzopoulos, G., Controlling earthQuakes (CoQuake) in the laboratory using pertinent fault stimulating techniques. PhD thesis, Ecole centrale de Nantes (2021). doi: <https://tel.archives-ouvertes.fr/tel-03670423>

[4] Gutiérrez-Ortíz, D., Tzortzopoulos, G., Stefanou, I., & Plestan, F. (2022). Earthquake Control: An Emerging Application for Robust Control. Theory and Experimental Tests. IEEE Transactions on Control Systems Technology. doi: <https://doi.org/10.1109/TCST.2023.3242431>

[5] Huang, Y., Wang, W., Liu, C., & Rosakis, A. J. (1998). Intersonic crack growth in bimaterial interfaces: an investigation of crack face contact. Journal of the Mechanics and Physics of Solids, 46(11), 2233-2259. [https://doi.org/10.1016/S0022-5096\(98\)00003-9](https://doi.org/10.1016/S0022-5096(98)00003-9)

[6] Latour, S., Gallot, T., Catheline, S., Voisin, C., Renard, F., Larose, E., & Campillo, M. (2011). Ultrafast ultrasonic imaging of dynamic sliding friction in soft solids: The slow slip and the super-shear regimes. Europhysics Letters, 96(5), 59003. doi: <https://doi.org/10.1209/0295-5075/96/59003>

Acknowledgments. The authors would like to acknowledge the support of the European Research Council (ERC) under the EUH 2020 program (Grant ID 757848 CoQuake).